

Exponential Functions

Chapter 6

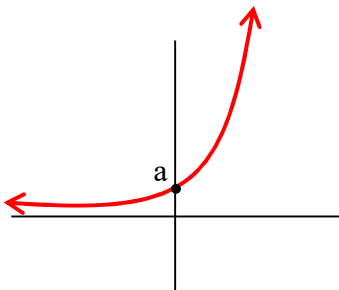
Exponential functions have the form: $y = a(b)^x$

a = y-intercept

b = base

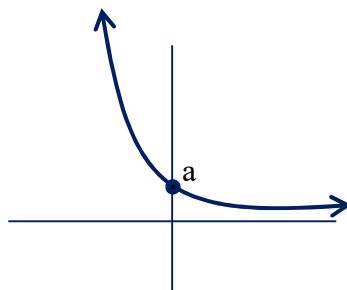
If the base is greater than 1,
the function increases.

If the base is between 0 and 1,
the function decreases.



b > 1

Exponential growth



0 < b < 1

Exponential decay

Growth Functions

The formula for exponential growth can be written like this:

$$\text{Amount} = \text{Starting amount} (1 + \text{growth rate})^t$$

Amount = Total number at time t

Starting amount = The number of things you started with

Growth rate = Can be written as a fraction (1/4) or a decimal percent (12% = 0.12)

t = time

For example, if there are 40 ducks on a lake and the population of ducks increases by $\frac{1}{5}$ every year, the function that models this is: $\text{Amount of ducks} = 40 \left(1 + \frac{1}{5}\right)^t$.

Decay Functions

The formula for exponential decay can be written like this:

$$\text{Amount} = \text{Starting amount} (1 - \text{decay rate})^t$$

Amount = Total number at time t

Starting amount = The number of things you started with

Decay rate = Can be written as a fraction (1/4) or a decimal percent (12% = 0.12)

t = time

For example, if a bar of soap weighs 200 grams and its weight decreases by 4% every time it is used, the function that models this is: $\text{Weight of soap} = 200 (1 - 0.04)^t$.